# 22397

## 23124 3 Hours / 70 Marks

Seat No.				

*Instructions*: (1) All Questions are *compulsory*.

- (2) Answer each Section on same / separate answer sheet.
- (3) Illustrate your answers with neat sketches wherever necessary.
- (4) Figures to the right indicate full marks.
- (5) Assume suitable data, if necessary.
- (6) Use of Non-programmable Electronic Pocket Calculator is permissible.

### 1. Attempt any FIVE of the following :

- (a) Determine the harmonic mean for the following data sets : 2, 5, 7 and 9.
- (b) Find the D6 for the following data :11, 25, 20, 15, 24, 28, 19, 21
- (c) For a distribution Karl Pearson's coefficient of skewness is 0.64, standard deviation is 13 and mean is 59.2. Find mode and median.
- (d) Calculate covariance for the following data :

Х	2.1	2.5	3.6	4.0
Y	8	10	12	14

- (e) In a single throw of a pair of dice, what is the probability of getting the sum a perfect square ?
- (f) If the random variable X follows a Poisson distribution with mean 3.4, find P(X = 6).
- (g) Random samples of size 225 are drawn from population with mean 100 and standard deviation 20. Find the mean and standard deviation of the sample mean.



Marks

10

#### 2. Attempt any THREE of the following :

- (a) If the average marks for a group of 30 girls are 80, the group of boys is 70 and the combined average is 76, how many boys are in the group ?
- (b) Find the median marks for the following distribution :

Classes	0-10	10-20	20-30	30-40	40-50
Frequency	2	12	22	8	6

(c) Following data gives the marks obtained by the student. Draw histogram and find modal marks obtained by student, check your result analytically :

Marks	51-60	61-70	71-80	81-90	91-100
No. of students	4	8	15	8	5

(d) Karl Pearson's coefficient of skewness for a data set is -0.6. If mean = 60 and S = 10, find median and mode for the data.

#### 3. Attempt any THREE of the following :

(a) Calculate the coefficient of skewness from the following data :

x	3	6	9	12	15	18
f	10	23	18	15	22	18

(b) Calculate Bowley's coefficient of skewness from the following data :

No. of children	2	4	6	8	10	12
No. of families	11	22	18	15	10	4

(c) Using least square method, fit the straight line Y = a + bx for following data :

x	1	2	3	4	5
У	0.5	1.7	3.4	5.7	8.4

(d) Calculate coefficient of correlation between *x* & y series from the following data :

x	1	3	5	6	7
у	4	2	1	3	5

#### 22397

12

#### 4. Attempt any THREE of the following :

(a) Calculate the coefficient of correlation for the following data :

Age of husband (x)	21	22	28	32	35	36
Age of wife (y)	18	20	25	30	31	32

(b) Fit the regression line for the data :

x	2	3	5	7	9
У	4	5	7	10	15

- (c) How many 3-digit even numbers can be made using the digits 1, 2, 3, 4, 6, 7 if no digit is repeated ?
- (d) A and B appear for an interview for two vacancies in the same post. The probability of A's selection is 1/6 and that of B's selection is 1/4. Find the probability that only one of them is selected.
- (e) John has two bags. Bag I has 7 red and 2 blue balls and bag II has 5 red and 9 blue balls. John draws a ball at random and it turns out to be red. Determine the probability that the ball was from the bag I using the Baye's theorem.

#### 5. Attempt any TWO of the following :

(a) (i) Attempt the following :

The probability that a mountain-bike travelling along a certain track will have a tyre burst is 0.05. Find probability that among 17 riders; exactly one has a burst tyre.

- (ii) The average number of earthquakes in a city is 3 per year. What is the probability that exactly 5 earthquakes will occur in a city next year ?
- (b) A manufacturer produces light-bulbs that are packed into boxes of 100. If quality control studies indicate that 0.5% of the light-bulbs produced are defective, what percentage of the boxes will contain 2 or more defectives ?
- (c) A manufacturer knows from experience that the resistance of resistors he produces is normal with mean  $\mu = 100$  ohms and standard deviation  $\sigma = 2$  ohms. What percentage of resistors will have resistance between 98 ohms and 102 ohms?

Given A(1) = 0.3413

12

### 6. Attempt any TWO of the following :

- (a) (i) A machine has produced washers having a thickness of 0.50 mm. A sample of 10 washers has an average thickness 0.53 with standard deviation 0.03 mm. Find the value of t using t-distribution.
  - (ii) In 120 throws of a single die the following distribution of faces was obtained. Find the value of  $\chi^2$  (chi square) :

Faces	1	2	3	4	5	6	Total
Frequencies	30	25	18	10	22	15	120

- (b) Test whether the sample having the values 63, 63, 64, 55, 66, 69, 70, 70, 71 has been chosen from a population with mean 65 at 5% level of significance (value of t for 8 degree of freedom is 2.31).
- (c) In an anti malaria campaign in a certain area, quinine was administered to 812 persons out of a total population of 3248. The number of fever cases is shown below :

Treatment	Fever	No fever	Total
Quinine	140	30	170
No Quinine	60	20	80
Total	200	50	250

Calculate the value of  $\chi^2$  (chi-square) and discuss the usefulness of quinine in checking malaria (Given for 1 degree of freedom value of  $\chi^2$  (chi square) at  $\alpha = 0.05$  level of significance 3.84).