22103

12425 3 Hours / 70 Marks

Seat No.

Instructions : (1) All Questions are *compulsory*.

- (2) Illustrate your answers with neat sketches wherever necessary.
- (3) Figures to the right indicate full marks.
- (4) Assume suitable data, if necessary.
- (5) Use of Non-programmable Electronic Pocket Calculator is permissible.
- (6) Mobile Phone, Pager and any other Electronic Communication devices are not permissible in Examination Hall.

1. Attempt any FIVE of the following :

- (a) Simplify $\log_2 14 \log_2 7$
- (b) Using determinant method find the area of triangle whose vertices are (4, 5) (0, 7) & (-1, 1).
- (c) Without using calculator find the value of $\cos (75^{\circ})$.
- (d) If the diagonals of a rhombus are 16 cm & 12 cm, find its area.
- (e) A cone and cylinder having the same area of the base and having also the same area of curved surfaces. If the height of the cylinder be 2 m, find the slant height of the cone.
- (f) The coefficient of variance of a certain distribution is 4 and mean is 125. Find standard deviation.
- (g) Find the range and coefficient of range of the following :80, 40, 120, 90, 50, 200, 180.



Marks

2. Attempt any THREE of the following :

(a) Find Inverse of matrix A, by adjoint method

where
$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 4 & 5 \\ 3 & 5 & 6 \end{bmatrix}$$

(b) Resolve into partial fraction,

$$\frac{x+3}{(x-1)(x+1)(x+5)}$$

(c) Using Cramer's rule, following equations are obtained as a result of an experiment :

 $P_1 + P_2 + P_3 = 6$; $P_2 + 3P_3 = 11$ and $P_1 - 2P_2 + P_3 = 0$.

Find value of P_1 , $P_2 \& P_3$.

(d) Calculate standard deviation and coefficient of variance from the following table :

Class Mark	7	8	9	10	11	12	13
Frequency	4	6	9	12	9	6	4

3. Attempt any THREE of the following :

(a) If
$$\tan \frac{\theta}{2} = \frac{2}{3}$$
, find value of '2 sin θ + 3 cos θ '.

(b) If $2 \cos 60^\circ \cdot \cos 10^\circ = \cos A + \cos B$

then find A and B.

(c) Simplify
$$\frac{\cos^2(180^\circ - \theta)}{\sin(-\theta)} + \frac{\cos^2(270^\circ - \theta)}{\sin(180^\circ - \theta)}$$

(d) Prove that
$$\frac{\sin 3A - \sin A}{\cos 3A + \cos A} = \tan A.$$

4. Attempt any THREE of the following :

(a) If $A = \begin{bmatrix} 2 & 4 \\ 1 & 1 \end{bmatrix}$ and $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$

then prove that $A^2 = 3A + 2I$.

(b) Resolve into partial fraction
$$\frac{3x-2}{(x+2)(x^2+4)}$$
.

(c) Prove that $8 \sin 20^\circ \cdot \sin 40^\circ \cos 10^\circ = \sqrt{3}$.

(d) Prove that
$$\frac{\cos 3A - \cos 7A}{\sin 9A + \sin A} = \cos 2A \tan 4A - \sin 2A$$
.

(e) If
$$\tan x = \frac{5}{6}$$
 and $\tan y = \frac{1}{11}$

show that $x + y = 45^{\circ}$.

5. Attempt any TWO of the following :

- (a) Attempt the following :
 - (i) Find the equation of the line whose x-intercept is 3 and y intercept is 4.
 - (ii) Find the equation of line passing through the point (2, 3) and having $slope\frac{1}{2}$.
- (b) Attempt the following :
 - (i) Find the equation of the line passing through (2, -3) and parallel to the line 4x y + 7 = 0.
 - (ii) Show that the point (1, 2) is equidistant from 4x 3y + 7 = 0 and 5x + 12y = 16.
- (c) Attempt the following :

Find the length of the longest pole that can be placed in a room 12 m long, 9 m broad and 8 m high.

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6. Attempt any TWO of the following :

(a) Solve the following equation by using matrix inversion method :

x + y + z = 6, 3x - y + 3z = 10, 5x + 5y - 4z = 3

(b) Find mean deviation about mean of the following distribution :

C.I.	10 - 20	20 - 30	30-40	40 - 50	50 - 60	60 - 70
Frequency	4	6	10	18	9	3

- (c) Attempt the following :
 - (i) Find range and co-efficient of range of the following :

C.I.	20 - 29	30 - 39	40 - 49	50 - 59	60 - 69	70 – 79
Frequency	10	15	30	20	15	10

(ii) The data gives mean weight and S.D. for two groups :

Group	Mean Weight	S.D.
А	80 kg	6.0 kg
В	60 kg	7.0 kg

Which of the two groups has greater variability ?