

314316

24225

3 Hours / 70 Marks

Seat No.

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- Instructions :**
- (1) All Questions are *compulsory*.
 - (2) Answer each next main Question on a new page.
 - (3) Illustrate your answers with neat sketches wherever necessary.
 - (4) Figures to the right indicate full marks.
 - (5) Assume suitable data, if necessary.
 - (6) Use of Non-programmable Electronic Pocket Calculator is permissible.
 - (7) Mobile Phone, Pager and any other Electronic Communication devices are not permissible in Examination Hall.

Marks

1. Attempt any FIVE of the following :

10

- (a) Two dice are thrown. What is probability of getting
 - (i) Double six
 - (ii) Sum of 8 or more dots.
- (b) A random variable is uniformly distributed over time interval 2 to 10. Find its variance.
- (c) Give any two objectives of Network analysis.
- (d) For the bivariate data $r = 0.3$, $\text{Cov}(X, Y) = 18$, $\sigma_x = 3$, find σ_y .
- (e) If $\sum d^2 = 66$ and $n = 10$, then find the rank correlation coefficient.



- (f) Find the coefficient of correlation and obtain the equation of the line of regression for the given data :

x	6	2	10	4	8
y	9	11	5	8	7

- (g) Two lines of regression are given by $8x - 10y + 66 = 0$ and $40x - 18y = 214$.

If $\sigma_x^2 = 9$, find :

- Mean values of x and y
- Coefficient of correlation between x and y .

2. Attempt any THREE of the following :

12

- A fair two dice are thrown. Find the probability that number on the upper face of the first die is 3 or sum of the numbers on their upper faces is 6.
- If $P(A) = 1/3$, $P(B) = 2/5$ and $P(A \cup B) = 8/15$, find :
 - $P(A/B)$
 - $P(A' \cap B')$
- Find the probability distribution of X :

X	1	2	3	4	5	6
F(X)	0.2	0.37	0.48	0.62	0.85	1

- Find $P(X \leq 3)$, $P(2 < X < 5)$
 - Find $P(X \leq 5)$, $P(X > 3)$
- (d) Explain three time estimates in PERT.

3. Attempt any THREE of the following :

12

- Two digits numbers are to be made using the digits 3, 5, 6 and 8 without repetition of digits. Find the probability of the following events :
 - The number is odd.
 - The number is divisible by 9.

- (b) For the probability distribution :

X	1	2	3	4	5
P (X = x)	0.2	0.4	0.1	0.1	0.2

Find : $E(X)$, $E(X^2)$, $\text{Var}(X)$

- (c) State Fulkerson's rule for numbering of events in a network diagram.

- (d) If for a bivariate data :

$\bar{x} = 10$, $\bar{y} = 12$, $v(X) = 9$, $\sigma_y = 4$ and $r = 0.6$, estimate y when $x = 5$.

4. Attempt any THREE of the following :

12

- (a) Find Spearman's Rank Co-efficient of correlation to the following data :

x	10	12	18	18	15	17	40
y	15	19	25	30	25	25	30

- (b) If X has Bernoulli distribution with $n = 20$, $P = 1/10$, find the mean $E(X)$ and Variance $V(X)$.

- (c) Explain latest start time and latest finish time. How are this determined ?

- (d) Find the rank correlation coefficient between x and y variables :

x	10	20	35	14	18	21	16
y	13	25	18	19	20	26	27

- (e) If the correlation coefficient between x and y is 0.6, covariance is 27 and variance of y is 25, find the variance of x .

5. Attempt any TWO of the following :

12

- (a) If a continuous random variable X follows exponentially distributed with parameter 2, find the value of K , there exists $P(X > K)/P(X \leq K) = a$.

- (b) Draw the AON (Activity On Arrow Network) diagram as well as Arrow diagram :

Activity	Immediate Predecessor	Activity	Immediate Predecessor
A	–	G	B, C
B	–	H	C
C	–	I	E, F
E	A	J	G, H
F	A, B	K	H

- (c) In a partially destroyed laboratory record of an analysis of regression data of the following data are legible :

Variance of $X = 9$, Regression equations :

$$8x - 10y + 66 = 0 \text{ and } 40x - 18y = 214$$

- The mean values of x and y .
- Correlation coefficient between x and y .
- Standard deviation of y .

6. Attempt any TWO of the following :

12

- (a) The following table gives the aptitude test scores and productivity indices of 10 workers selected at random :

- Obtain the two regression equations and
- Obtain the line of regression to predict X for $Y = 75$

X	60	62	65	70	72	48	53	73	65	82
Y	68	60	62	80	85	40	52	62	60	81

- (b) Find the equation of line of regression of Y on X and X on Y for the following data :

$$n = 10, \sum(x_i - \bar{x})(y_i - \bar{y}) = 1220.$$

$$\sigma_x^2 = 130, \sigma_y^2 = 165. \text{ Estimate } Y \text{ For } X = 40.$$

- (c) Calculate Karl Pearson's coefficient of correlation from the following data :

x	11	10	9	8	7	6	5
y	20	18	12	8	10	5	4