



SUMMER– 19 EXAMINATION

Subject Name: DESIGN OF R.C.C. STRUCTURES

Model Answer

Subject Code: 17604

Important Instructions to examiners:

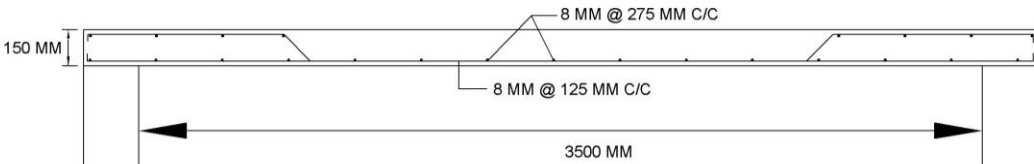
- 1) The answers should be examined by key words and not as word-to-word as given in the model answer scheme.
- 2) The model answer and the answer written by candidate may vary but the examiner may try to assess the understanding level of the candidate.
- 3) The language errors such as grammatical, spelling errors should not be given more Importance (Not applicable for subject English and Communication Skills).
- 4) While assessing figures, examiner may give credit for principal components indicated in the figure. The figures drawn by candidate and model answer may vary. The examiner may give credit for any equivalent figure drawn.
- 5) Credits may be given step wise for numerical problems. In some cases, the assumed constant values may vary and there may be some difference in the candidate's answers and model answer.
- 6) In case of some questions credit may be given by judgement on part of examiner of relevant answer based on candidate's understanding.
- 7) For programming language papers, credit may be given to any other program based on equivalent concept.

Q. No.	Sub Q. N.	Answers	Marking Scheme
Q.1	(A) (a) Ans	<p>Solve any THREE:</p> <p>Explain the concept of limit state of flexure. State various limit states.</p> <p>Concept of limit state of flexure: It is to achieve an acceptable probability that a structure will not collapse in flexure in its life time, that is, it will not reach limit state of collapse (Flexure).</p> <p>Various limit states:</p> <ol style="list-style-type: none"> 1. Limit state of collapse- <ol style="list-style-type: none"> i. Flexure/Bending. ii. Shear. iii. Torsion. iv. Axial load (Tension and compression). 2. Limit state of Serviceability- <ol style="list-style-type: none"> i. Deflection. ii. Cracking. iii. Vibration. 	<p>(12)</p> <p>02 M</p> <p>01 M</p> <p>01 M</p>
Q.1	(A)(b) Ans	<p>Define 'characteristic strength' and 'characteristic load'.</p> <p>Characteristic strength: It is the value of the strength of material below which not more than 5 percent of the test results are expected to fall.</p> <p>Characteristic load: It is the value of load which has a 95 percent probability of not being exceeded during the life of the structure.</p>	<p>02 M</p> <p>02 M</p>
Q.1	(A)(c) Ans	<p>Write the requirements of ductility for flexural members as per IS: 13920-1993.</p> <p>Requirements of ductility for flexural members.</p> <ol style="list-style-type: none"> 1. The factored axial stress on the member under earthquake loading shall not exceed 0.1 f_{ck}. 2. The member shall preferably have a width-to-depth ratio of more than 0.3. 3. The width of the member shall not be less than 200 mm. 4. The depth D of the member shall preferably be not more than l/4 of the clear 	<p>01 M for each</p>



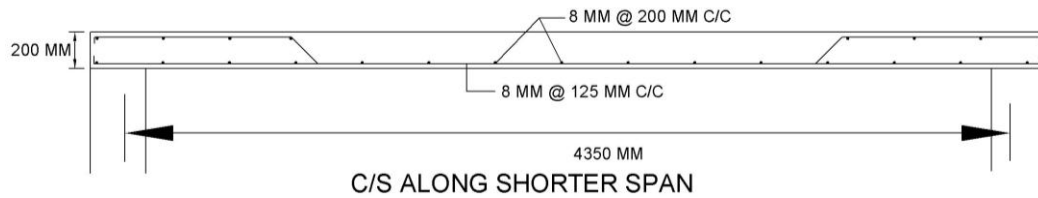
		span.	
Q.1	(A)(d) Ans	<p>Explain pre-tensioning and post-tensioning.</p> <p>Pre-tensioning method: It is done by stressing wires or strands, called tendons, to predetermine amount by stretching them between two anchorages called abutments prior to placing the concrete. The concrete is then placed and tendons become bonded to concrete throughout their length. After the concrete has hardened, the tendons are released by cutting them at the anchorages. The tendons tend to regain their original length by shortening and transfer compressive stress to concrete through bond.</p> <p>Post-tensioning method: In this method first tendons are placed in position passing through flexible tube then concrete is placed in the mould. After gaining strength by concrete, tendons are stretched against concrete itself and then anchored at both ends. In this method, stress is transferred through bearing at ends of tendons.</p>	02 M 02 M
Q.1	(A)(e) Ans	<p>State various forms of shear reinforcement in beams.</p> <p>Shear reinforcement in beams can be provided in any one of the forms given below.</p> <ol style="list-style-type: none"> 1. Vertical stirrups. 2. Inclined stirrups. 3. Bent up bars with stirrups. 	04 M
Q.1	(B) (a) Ans	<p>Solve any ONE:</p> <p>A beam having dimension 230 x 450 mm effective is reinforced with 4 bars of 16 mm diameter on tension side. Calculate the ultimate moment of resistance of the beam if M20 grade concrete and Fe415 steel are used.</p> <p>$b = 230 \text{ mm}$, $d = 450 \text{ mm}$, $A_{st} = 16 \text{ mm}-4 \text{ bars.}$, M-20, Fe-415, $\mu_u = ?$</p> $A_{st} = 4 \times \pi \times \phi^2 / 4$ $= 4 \times \pi \times 16^2 / 4 = 804.25 \text{ mm}^2$ <p>Actual neutral axis $x_u = (0.87 \times f_y \times A_{st}) / (0.36 \times f_{ck} \times b)$</p> $= (0.87 \times 415 \times 804.25) / (0.36 \times 20 \times 230)$ $= 175.35 \text{ mm.}$ $x_{u\max} = 0.48 \times d$ $= 0.48 \times 450$ $= 216 \text{ mm.}$ <p>$x_u < x_{u\max}$, hence beam is under reinforced.</p> $\mu_u = 0.87 \times f_y \times A_{st} (d - 0.42x_u)$ $= 0.87 \times 415 \times 804.25 (450 - 0.42 \times 175.35)$ $= 109.28 \times 10^6 \text{ N-mm.}$ <p style="text-align: center;">OR</p> $\mu_u = 0.36 \times f_{ck} \times b \times x_u (d - 0.42x_u)$ $= 0.36 \times 20 \times 230 \times 175.35 (450 - 0.42 \times 175.35)$ $= 109.28 \times 10^6 \text{ N-mm}$	(06) 01 M 01 M 01 M 01 M 02 M
Q.1	(B)(b) Ans	<p>A beam 300 mm x 500 mm effective size carries a factored bending moment of 175 kN-m. If concrete M20 & Steel grade Fe500 are used, find area of steel required.</p> <p>$b = 300 \text{ mm}$, $d = 500 \text{ mm}$, $\mu_u = 175 \text{ kN-m}$, M-20, Fe-500, $A_{st} = ?$</p> $\mu_{lim} = 0.134 \times f_{ck} \times b \times d^2$ $= 0.134 \times 20 \times 300 \times 500^2$ $= 201 \times 10^6 \text{ N-mm}$ <p>$\mu_u < \mu_{lim}$, Hence beam is Under reinforced.</p> $A_{st} = 0.5 \times f_{ck} \times b \times d \{1 - \text{SQRT}[1 - (4.6 \times \mu_u) / (f_{ck} \times b \times d^2)]\} / f_y$	02 M 01 M 01 M



		$= 0.5 \times 20 \times 300 \times 500 \{1 - \text{SQRT}[1 - (4.6 \times 175 \times 10^6) / (20 \times 300 \times 500^2)]\} / 500$ $= 957.94 \text{ mm}^2$.	01 M 01 M
Q.2	(a)	Solve any TWO: Design one way slab with following data, width of support = 230 mm, clear span = 3.5 m, Live load = 2 kN/m², Floor finish = 1 kN/m², concrete M20 & steel 415, M.F. = 1.4. Sketch c/s of slab showing reinforcement details (No checks are required)	(16)
	Ans	Support width = 230 mm, Clear span = 3.5 m, L.L. = 2 kN/m ² , F.F. = 1 kN/m ² , M-20, Fe-415, M.F. = 1.4. Depth of slab required = span / (M.F. x 20) $= 3500 / (1.4 \times 20)$ $= 125 \text{ mm}.$ Assuming cover 25 mm, (Note: Students may assume different cover) D = 125 + 25 = 150 mm. Effective span: 1) Clear span + d = 3.5 + 0.125 = 3.625 m. 2) Clear span + support width = 3.5 + 0.23 = 3.73 m. Lesser is 3.625 m. Hence le = 3.625 m. Loading: 1) Live load = 2.0 kN/m ² 2) Floor finish = 1.0 kN/m ² 3) Self weight = 0.15 x 25 = 3.75 kN/m ² Total = 6.75 kN/m ² Factored load = 1.5 x 6.75 = 10.125 kN/m ² Mu = 10.125 x 3.625 ² / 8 16.63 kN-m. Depth required for strength = SQRT[Mu / (0.138 x fck x b)] $= \text{SQRT}[16.63 \times 10^6 / (0.138 \times 20 \times 1000)]$ $= 77.62 \text{ mm} < \text{assumed hence O.K.}$ Provide D = 150 mm d = 125 mm. Ast = 0.5 x fck x b x d {1 - SQRT[1 - (4.6 x Mu) / (fck x b x d ²)]} / fy $= 0.5 \times 20 \times 1000 \times 125 \{1 - \text{SQRT}[1 - (4.6 \times 16.63 \times 10^6) / (20 \times 1000 \times 125^2)]\} / 415$ $= 394.5 \text{ mm}^2.$ Providing 8 mm dia. Bars Area of one bar A1 = $\pi \times \phi^2 / 4 = \pi \times 8^2 / 4 = 50.27 \text{ mm}^2$ (Note: Students may assume different bar dia.) Spacing = 1000 x A1 / Ast $= 1000 \times 50.27 / 394.5 = 127.4 \text{ mm}.$ Provide 8 mm dia. @ 125 mm c/c. Distribution steel: Area = 0.12 x 1000 x 150 / 100 $= 180 \text{ mm}^2.$ Spacing for 8 mm dia. Bars = 1000 x 50.27 / 180 = 279.3 mm Provide 8 mm dia. @ 275 mm c/c.	01 M 01 M 01 M 01 M 01 M 01 M 01 M 01 M
			Fig. 02 M



Q.2	(b)	<p><i>Design a reinforced concrete slab panel for 6.55 m x 4.35 m simply supported on all four sides. It carries a live load 2 kN/m² & Floor finish load 1.0 kN/m². Use M20 concrete & Fe415 steel. Sketch the c/s of slab along shorter span showing steel details (No checks). Use $\alpha_x = 0.104$, $\alpha_y = 0.046$. M.F. = 1.3.</i></p> <p>Ans Shorter span = 4.35 m, Longer span = 6.55 m, L.L. = 2 kN/m², F.F. = 1 kN/m², M-20, Fe-415, M.F. = 1.3, $\alpha_x = 0.104$, $\alpha_y = 0.046$.</p> <p>Aspect ratio = Longer span / Shorter span = 6.55 / 4.35 = 1.51 < 2.0 Hence Two way slab. Depth of slab required = shorter span / (M.F. x 20) = 4350 / (1.3 x 20) = 167.31 mm.</p> <p>Assuming cover 25 mm, (Note: Students may assume different cover) D = 167.31 + 25 = 192.3 mm. Assume overall depth (D) = 200 mm and Effective depth (d) = 175 mm.</p> <p>Loading: 1) Live load = 2.0 kN/m² 2) Floor finish = 1.0 kN/m² 3) Self weight = 0.20 x 25 = 5.0 kN/m² Total = 8.0 kN/m²</p> <p>Factored load = 1.5 x 8.0 = 12.0 kN/m²</p> <p>Ultimate bending moment calculations: M_{ux} = $\alpha_x \times w_u \times l_x^2$ = 0.104 x 12 x 4.35² = 23.62 kN-m M_{uy} = $\alpha_y \times w_u \times l_y^2$ = 0.046 x 12 x 6.55² = 10.45 kN-m.</p> <p>Depth required for strength = $\text{SQRT}[M_{ux} / (0.138 \times f_{ck} \times b)]$ = $\text{SQRT}[23.62 \times 10^6 / (0.138 \times 20 \times 1000)]$ = 92.51 mm < assumed hence O.K.</p> <p>Provide D = 200 mm dx = 175 mm. and dy = 175 – 10 = 165 mm (assuming bar dia. 10 mm)</p> <p>A_{stx} = $0.5 \times f_{ck} \times b \times dx \{1 - \text{SQRT}[1 - (4.6 \times M_{ux}) / (f_{ck} \times b \times dx^2)]\} / f_y$ = $0.5 \times 20 \times 1000 \times 175 \{1 - \text{SQRT}[1 - (4.6 \times 23.62 \times 10^6) / (20 \times 1000 \times 175^2)]\} / 415$ = 392.3 mm².</p> <p>Providing 8 mm dia. Bars Area of one bar A₁ = $\pi \times \phi^2 / 4 = \pi \times 8^2 / 4 = 50.27 \text{ mm}^2$ (Note: Students may assume different bar dia.)</p> <p>Spacing = 1000 x A₁ / A_{st} = 1000 x 50.27 / 392.3 = 128 mm.</p> <p>Provide 8 mm dia. @ 125 mm c/c along shorter span.</p> <p>A_{sty} = $0.5 \times f_{ck} \times b \times dy \{1 - \text{SQRT}[1 - (4.6 \times M_{uy}) / (f_{ck} \times b \times dy^2)]\} / f_y$ = $0.5 \times 20 \times 1000 \times 165 \{1 - \text{SQRT}[1 - (4.6 \times 10.45 \times 10^6) / (20 \times 1000 \times 165^2)]\} / 415$ = 179.6 mm².</p> <p>Minimum A_{st} = 0.12 x 1000 x 200 / 100 = 240 mm². A_{sty} < Min. A_{st}, Hence provide minimum A_{st}.</p> <p>Providing 8 mm dia. Bars Area of one bar A₁ = $\pi \times \phi^2 / 4 = \pi \times 8^2 / 4 = 50.27 \text{ mm}^2$ (Note: Students may assume different bar dia.)</p> <p>Spacing = 1000 x A₁ / A_{st} = 1000 x 50.27 / 240 = 209.5 mm.</p> <p>Provide 8 mm dia. @ 200 mm c/c along longer span.</p>	01 M 01 M 01 M 01 M 01 M 01 M 01 M
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01 M for fig.

Q.2 (c) **Design a cantilever slab for Chajja with following data. Span = 1.5 m, L.L. = 2 kN/m², F.F. = 0.5 kN/m², Adopt M20 & Fe415, Modification factor = 1.3.**

Ans Span = 1.5 m, L.L. = 2 kN/m², F.F. = 0.5 kN/m², M-20, Fe-415, M.F. = 1.3.

$$\begin{aligned} \text{Depth of slab required} &= \text{span} / (\text{M.F.} \times 7) \\ &= 1500 / (1.3 \times 7) \\ &= 164.8 \text{ mm.} \end{aligned}$$

Assuming cover 25 mm, **(Note: Students may assume different cover)**

$$D = 164.8 + 25 = 189.8 \text{ mm.}$$

Assume overall depth = 190 mm and effective depth = 165 mm.

Effective span:

$$1) \text{ Clear span} + d/2 = 1.5 + 0.165/2 = 1.5825 \text{ m. (Note: Students may consider given span as effective span)}$$

Loading:

$$1) \text{ Live load} = 2.0 \text{ kN/m}^2$$

$$2) \text{ Floor finish} = 0.5 \text{ kN/m}^2$$

$$3) \text{ Self weight} = 0.19 \times 25 = 4.75 \text{ kN/m}^2$$

$$\text{Total} = 7.25 \text{ kN/m}^2$$

$$\text{Factored load} = 1.5 \times 7.25 = 10.875 \text{ kN/m}^2$$

$$M_u = 10.875 \times 1.5825^2 / 2$$

$$= 13.62 \text{ kN-m.}$$

$$\text{Depth required for strength} = \text{SQRT}[M_u / (0.138 \times f_{ck} \times b)]$$

$$= \text{SQRT}[13.62 \times 10^6 / (0.138 \times 20 \times 1000)]$$

$$= 70.25 \text{ mm} < \text{assumed hence O.K.}$$

Provide D = 190 mm

$$d = 175 \text{ mm.}$$

$$A_{st} = 0.5 \times f_{ck} \times b \times d \{1 - \text{SQRT}[1 - (4.6 \times M_u) / (f_{ck} \times b \times d^2)]\} / f_y$$

$$= 0.5 \times 20 \times 1000 \times 175 \{1 - \text{SQRT}[1 - (4.6 \times 13.62 \times 10^6) / (20 \times 1000 \times 175^2)]\} / 415$$

$$= 235.7 \text{ mm}^2.$$

$$\text{Minimum } A_{st} = 0.12 \times 1000 \times 190 / 100 = 228 \text{ mm}^2.$$

$A_{st} > \text{Min. } A_{st}$, Hence O.K.

$$\text{Providing 8 mm dia. Bars Area of one bar } A_1 = \pi \times \phi^2 / 4 = \pi \times 8^2 / 4 = 50.27 \text{ mm}^2$$

(Note: Students may assume different bar dia.)

$$\text{Spacing} = 1000 \times A_1 / A_{st}$$

$$= 1000 \times 50.27 / 235.7 = 213.3 \text{ mm.}$$

Provide 8 mm dia. @ 210 mm c/c.

$$\text{Distribution steel: Area} = 0.12 \times 1000 \times 190 / 100$$

$$= 228 \text{ mm}^2.$$

$$\text{Spacing for 8 mm dia. Bars} = 1000 \times 50.27 / 228 = 220.5 \text{ mm}$$

Provide 8 mm dia. @ 220 mm c/c.

01 M

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01 M

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02 M

02 M

Q.3 **Attempt any FOUR:**

(16)



	(a)	What is flange width of T-beam as per IS: 456? State meaning of each term used therein.	
	Ans	Flange width of T-beam = $(l_0/6) + b_w + 6D_f$ but not greater than the width of web plus half the sum of the clear distance to the adjacent beams on either side. l_0 = Distance between points of zero moments in the beam. b_w = width of web. D_f = Depth of flange.	02 M 02 M
Q.3	(b)	Find the moment of resistance of (T) beam with following data: $D_f = 100$ mm, $b_f = 1200$ mm, $b_w = 250$ mm, $d = 500$ mm, $A_{st} = 1600$ mm², M25 concrete and Fe415 steel.	
	Ans	$D_f = 100$ mm, $b_f = 1200$ mm, $b_w = 250$ mm, $d = 500$ mm, $A_{st} = 1600$ mm ² , M-25, Fe-415. Actual neutral axis $x_u = (0.87 \times f_y \times A_{st}) / (0.36 \times f_{ck} \times b_f)$ $= (0.87 \times 415 \times 1600) / (0.36 \times 25 \times 1200)$ $= 53.49$ mm. $X_{u\max} = 0.48 \times d$ $= 0.48 \times 500$ $= 240$ mm. $X_u < x_{u\max}$, hence beam is under reinforced. $M_u = 0.87 \times f_y \times A_{st} (d - 0.42x_u)$ $= 0.87 \times 415 \times 1600 (500 - 0.42 \times 53.49)$ $= 275.9 \times 10^6$ N-mm.	01 M 01 M 02 M
		OR	
		$M_u = 0.36 \times f_{ck} \times b_f \times x_u (d - 0.42x_u)$ $= 0.36 \times 25 \times 1200 \times 53.49 (500 - 0.42 \times 53.49)$ $= 275.9 \times 10^6$ N-mm	
Q.3	(c)	Diameter of steel bar is 16 mm, Use Fe415 and design bond stress is 1.2 mPa. For plain bar in tension. Find development length in tension and compression.	
	Ans	$\phi = 16$ mm, Fe-415, Design bond stress = 1.2 mPa. Bond stress for deformed bars in tension = $1.2 \times 1.6 = 1.92$ mPa. Bond stress for deformed bars in compression = $1.2 \times 1.6 \times 1.25 = 2.4$ mPa. Development length in tension = $0.87 \times 415 \times 16 / (4 \times 1.92) = 752.2$ mm. Development length in compression = $0.87 \times 415 \times 16 / (4 \times 2.4) = 601.75$ mm.	01 M 01 M 01 M 01 M
Q.3	(d)	Define the development length. How it is calculated.	
	Ans	Development length: It is an additional length of a bar of given diameter that required beyond a section for proper anchorage through bond. Development length is calculated using following expression. $l_d = \text{Actual stress in steel} \times \phi / 4 \times \text{design bond stress.}$	02 M 02 M
Q.3	(e)	Design an axially loaded column 400 mm x 400 mm pinned at both ends with an unsupported length of 3 m for carrying a factored load of 2500 kN. Use M20 grade concrete and Fe415 steel.	(16)
	Ans	Column 400 mm x 400 mm, $l_e = 3$ m, $P_u = 2500$ kN, M-20, Fe-415. $A_g = 400 \times 400 = 160000$ mm ² $A_c = A_g - A_{sc} = 160000 - A_{sc}$ $P_u = (0.4 \times f_{ck} \times A_c) + (0.67 \times f_y \times A_{sc})$ $2500 \times 10^3 = [0.4 \times 20 \times (160000 - A_{sc})] + (0.67 \times 415 \times A_{sc})$ $= 1280000 - 8A_{sc} + 278.05A_{sc}$ $A_{sc} = (2500 \times 10^3 - 1280000) / 270.05$	01 M 01 M



		<p>$= 4517.7 \text{ mm}^2$. Min. Asc = $0.8 \times 400 \times 400 / 100 = 1280 \text{ mm}^2$. Max. Asc = $6 \times 400 \times 400 / 100 = 9600 \text{ mm}^2$. Min. Asc < Asc < Max. Asc Hence O. K. Provide 22 mm dia. 12 bars. (Note: Students may provide different combination of no. and dia. Of bars.)</p> <p>Lateral Ties: Diameter of bar: (Greater of below) i. $\frac{1}{4}$ of main bar dia. = $22/4 = 5.5 \text{ mm}$ ii. 6 mm. Provide 6 mm dia. bars. Pitch: (Least of below) i. 16 times dia. Of main bar = $16 \times 22 = 352 \text{ mm}$. ii. Least lateral dim. = 400 mm. iii. 300 mm. Provide pitch 300 mm. Hence provide 6 mm dia. @ 300 mm c/c.</p>	<p>01 M</p> <p>01 M</p>
Q.4	(A) (a) Ans	<p>Attempt any THREE: State any four losses in pre-stressing and describe any one. Losses in pre-stressing: 1. Due to elastic shortening. 2. Due to creep of concrete. 3. Due to shrinkage of concrete. 4. Due to relaxation of steel. 5. Due to friction. 6. Due to slip of anchorages.</p> <p>1. Elastic shortening: When pre-stress is applied to the concrete, an elastic shortening of concrete takes place. This results in an equal and simultaneous shortening of pre-stressing steel. This loss occurs in pre-tensioning method while in post-tensioning method this loss can be avoided by stretching all tendons simultaneously.</p> <p>2. Creep of concrete: Creep is the property of concrete by which it continues to deform with time under sustained load at unit stresses within the accepted elastic range. Due to creep, shortening of concrete takes place. This results in an equal and simultaneous shortening of pre-stressing steel.</p> <p>3. Shrinkage of concrete: Shrinkage is defined as decrease in volume of concrete due to loss in moisture. Due to shrinkage, shortening of concrete takes place. This results in an equal and simultaneous shortening of pre-stressing steel.</p> <p>4. Relaxation of steel: Relaxation is assumed to mean the loss of stress in steel under nearly constant strain at constant temperature. It is similar to creep of concrete.</p> <p>5. Friction: This loss occurs only in post-tensioning method. There are small frictional losses in the jacking equipment. There is also friction between tendons and surrounding materials.</p> <p>6. Slip of anchorages: This loss occurs only in post-tensioning method. After stretching and anchoring, tendons are released and the force is transferred to the anchorages. Due to this load, anchorages pierce in the concrete resulting</p>	<p>(12)</p> <p>Any four 01/2 M for each</p> <p>Any one 02 M</p>



		shortening of tendons. This shortening of tendons results in decreasing stress in tendons.	
Q.4	(A)(b)	Calculate working load carrying capacity of column 300 mm x 450 mm in dimension and provided with 8-16 mm diameter bars. Use M20 & Fe500 steel.	
	Ans	Column 300 mm x 450 mm, M-20, Fe-500, Asc = 16 mm dia. 8 bars. $A_g = 300 \times 450 = 135000 \text{ mm}^2$ $A_{sc} = 8 \times \pi \times 16^2 / 4 = 1608.5 \text{ mm}^2$ $A_c = A_g - A_{sc} = 135000 - 1608.5 = 133391.5$ $P_u = (0.4 \times f_{ck} \times A_c) + (0.67 \times f_y \times A_{sc})$ $= (0.4 \times 20 \times 133391.5) + (0.67 \times 500 \times 1608.5)$ $= 1605979.5 \text{ N} = 1605.98 \text{ kN}.$ Working load = $P_u / \text{F.O.S.}$ $= 1605.98 / 1.5$ $= 1070.65 \text{ kN}$	01 M 02 M 01 M
Q.4	(A)(c)	State the values of partial factor of safety for steel and concrete.	
	Ans	1) Partial factor of safety for steel = 1.15 2) Partial factor of safety for concrete = 1.5	02 M 02 M
Q.4	(A)(d)	State four situations where doubly reinforced section is preferred.	
	Ans	Situations where doubly reinforced section is preferred. 1. When depth of beam is restricted and strength of beam having restricted depth is inadequate. 2. When the section are subjected to reversal of bending moment. 3. In continuous T-beam where the portion of beam over intermediate supports has to be designed as doubly reinforced. 4. When the beams are subjected to eccentric loading, shocks or impact loads.	01 M for each
Q.4	(B)	Attempt any ONE:	(06)
	(a)	An R.C.C. beam 230 mm x 450 mm effective is subjected to a factored moment of 140 kN-m. Calculate area of steel in tension and compression zone. Use M20 gradt concrete & Fe415 steel. (Assume d' 45 mm and $d'/d = 0.1$, $f_{sc} = 353 \text{ N/mm}^2$)	
	Ans	$b = 230 \text{ mm}$, $d = 450 \text{ mm}$, $M_u = 140 \text{ kN-m}$, M-20, Fe-415, $d' = 45 \text{ mm}$, $f_{sc} = 353 \text{ N/mm}^2$. $M_{u1} = 0.138 \times f_{ck} \times b \times d^2$ $= 0.138 \times 20 \times 230 \times 450^2$ $= 128.547 \times 10^6 \text{ N-mm}.$ $M_{u2} = 140 \times 10^6 - 128.547 \times 10^6$ $= 11.453 \times 10^6 \text{ N-mm}$ $X_{u\max} = 0.48 \times 450 = 216 \text{ mm}.$ $A_{st1} = M_{u1} / [0.87 \times f_y \times (d - 0.42 x_{u\max})]$ $= 128.547 \times 10^6 / [0.87 \times 415 \times (450 - 0.42 \times 216)]$ $= 990.97 \text{ mm}^2$ $A_{sc} = M_{u2} / [f_{sc} \times (d - d')]$ $= 11.453 \times 10^6 / [353 \times (450 - 45)]$ $= 80.11 \text{ mm}^2.$ $A_{st2} = M_{u2} / [0.87 \times f_y \times (d - d')]$ $= 11.453 \times 10^6 / [0.87 \times 415 \times (450 - 45)]$ $= 78.3 \text{ mm}^2.$	01 M 01 M 01 M 01 M
		OR	
		$A_{st2} = (f_{sc} \times A_{sc}) / (0.87 \times f_y)$ $= (353 \times 80.11) / (0.87 \times 415)$	01 M



		$= 78.3 \text{ mm}^2$. Total Ast = $990.97 + 78.3 = 1069.27 \text{ mm}^2$.	01 M
Q.4	(B)(b)	<p>A beam 240 mm x 500 mm effective, it is reinforced with 4-16 mm diameter tension side and 2-12 mm in compression zone, each an effective cover of 40 mm. Use M20 concrete & Fe415 steel. Find ultimate moment of resistance. Assume $f_{sc} = 352 \text{ N/mm}^2$.</p> <p>Ans $b = 240 \text{ mm}$, $d = 500 \text{ mm}$, $A_{st} = 16 \text{ mm} - 4$, $A_{sc} = 12 \text{ mm} - 2$, M-20, Fe-415, $d' = 40 \text{ mm}$, $f_{sc} = 352 \text{ N/mm}^2$.</p> $A_{st} = 4 \times \pi \times \phi^2 / 4$ $= 4 \times \pi \times 16^2 / 4 = 804.25 \text{ mm}^2$ $A_{sc} = 2 \times \pi \times \phi^2 / 4$ $= 2 \times \pi \times 12^2 / 4 = 226.19 \text{ mm}^2$ <p>Actual neutral axis $x_u = [(0.87 \times f_y \times A_{st}) - (f_{sc} \times A_{sc})] / (0.36 \times f_{ck} \times b)$ $= [(0.87 \times 415 \times 804.25) - (352 \times 226.19)] / (0.36 \times 20 \times 240)$ $= 121.97 \text{ mm}$.</p> $x_{u\max} = 0.48 \times d$ $= 0.48 \times 500$ $= 240 \text{ mm}$. $x_u < x_{u\max}$, hence beam is under reinforced. $M_u = 0.36 \times f_{ck} \times b \times x_u (d - 0.42x_u) + f_{sc} \times A_{sc} (d - d')$ $= 0.36 \times 20 \times 240 \times 121.97 (500 - 0.42 \times 121.97) + 352 \times 226.19 (500 - 40)$ $= 131.21 \times 10^6 \text{ N-mm}$.	01 M 01 M 02 M 01 M 02 M
Q.5	(a)	<p>Attempt any TWO: Design a doubly reinforced rectangular beam 300 mm x 660 mm overall size, for an effective span of 5 m. The beam is subjected to udl of 55 kN/m. Assume effective cover 60 mm. Use M20 & Fe415 steel. $d'/d = 0.1$, $f_{sc} = 353 \text{ N/mm}^2$.</p> <p>Ans $L_e = 5 \text{ m}$., $w = 55 \text{ kN/m}$, $b = 300 \text{ mm}$, $D = 660 \text{ mm}$, M-20, Fe-415, $d' = 60 \text{ mm}$, $f_{sc} = 353 \text{ N/mm}^2$.</p> <p>Factored load = $1.5 \times 55 = 82.5 \text{ kN/m}$</p> $M_u = 82.5 \times 5^2 / 8$ $= 257.81 \text{ kN-m}$. <p>Effective depth $d = 660 - 60 = 600 \text{ mm}$.</p> $M_{ulim} = 0.138 \times 20 \times 300 \times 600^2$ $= 298.08 \text{ kN-m}$ $M_u < M_{ulim}$, Hence singly under reinforced beam is to be designed. $A_{st} = 0.5 \times f_{ck} \times b \times d \{1 - \text{SQRT}[1 - (4.6 \times M_u) / (f_{ck} \times b \times d^2)]\} / f_y$ $= 0.5 \times 20 \times 300 \times 600 \{1 - \text{SQRT}[1 - (4.6 \times 257.812 \times 10^6) / (20 \times 300 \times 600^2)]\} / 415$ $= 235.71424.7 \text{ mm}^2$	01 M 02 M 01 M 01 M 01 M 02 M
Q.5	(b)	<p>A beam 250 mm x 400 mm deep effective is reinforced with 3 bars of 16 mm diameter of grade Fe415. The shear force at the support is 60 kN. Design the shear reinforcement if grade of concrete used is M20. Use 6 mm or 8 mm diameter vertical stirrups.</p> <p>Ans $b = 250 \text{ mm}$, $d = 400 \text{ mm}$, $A_{st} = 16 - 3$, Fe-415, $V = 60 \text{ kN}$, M-20.</p> $V_u = 1.5 \times 60 = 90 \text{ kN}$ <p>Nominal shear stress = $V_u / (b \times d)$ $= 90 \times 10^3 / (250 \times 400)$ $= 0.9 \text{ N/mm}^2$</p> $A_{st} = 3 \times \pi \times 16^2 / 4 = 603.19 \text{ mm}^2$ $P_t\% = 603.19 \times 100 / (25 \times 400) = 0.60\%$	01 M 01 M



Note: Values of permissible shear stress are not given; hence students may assume different values. Hence accordingly marks shall be given)

Pt%	0.50	0.75
Permissible shear stress N/mm ²	0.48	0.56

For 0.6%, Permissible shear stress = $0.48 + \left\{ \frac{(0.56 - 0.48)}{(0.75 - 0.50)} \times (0.60 - 0.50) \right\}$
= 0.512 N/mm²

Nominal shear stress > permissible shear stress, hence shear reinforcement is to be designed.

$V_{us} = V_u - \text{permissible shear stress} \times b \times d$
= $90 \times 10^3 - (0.512 \times 250 \times 400)$
= 38800 N.

	For 6 mm dia. Stirrups	For 8 mm dia. stirrups
$A_{sv} = 2 \times \pi \times \phi^2 / 4$	56.54 mm ²	100.54 mm ²
Spacing = $0.87 \times f_y \times A_{sv} \times d / V_{us}$	210.5 mm	374.23 mm
Spacing for min. stirrups = $(0.87 \times f_y \times A_{sv}) / (0.4 \times b)$	204 mm	363 mm
Max. spacing 0.75 d or 300 mm whichever lesser.	300 mm 300 mm	300 mm 300 mm
Provide	6 mm dia. @ 200 mm c/c	8 mm dia. @ 300 mm c/c

01 M

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Q.5

(c)

Design an isolated square footing for a square reinforced concrete column section 250 mm size to carry an axial factored load 700 kN. The S.B.C. of the soil is 150 kN/m². Calculate the depth and steel required of footing from bending moment consideration only. Show reinforcement details. Use M20 & Fe415.

Ans

Column 250 mm x 250 mm, $P_u = 700$ kN, SBC of soil = 150 kN/m², M-20, Fe-415.

Note: Students may assume ultimate bearing capacity as 1.5 times or 2 times SBC.

Ultimate bearing capacity	1.5 x 150 = 225 kN/m ²	2.0 x 150 = 300 kN/m ²
Self-weight of footing = 5% of load on column.	35 kN	35 kN
Total ultimate load on soil	735 kN	735 kN
Area of footing required = Total ultimate load on soil / Ultimate bearing capacity of soil	$735 / 225 = 3.27 \text{ m}^2$	$735 / 300 = 2.45 \text{ m}^2$
Size = SQRT(Area)	1.81 m	1.565 m.
Provide size	1.85 m x 1.85 m	1.6 m x 1.6 m
Actual area provided	3.4225 m ²	2.56 m ²
Net ultimate upward pressure (q _{nu}) = Ultimate load on column / Actual area provided	$700 / 3.4225 = 204.5 \text{ kN/m}^2$	$700 / 2.56 = 273.5 \text{ kN/m}^2$
Projection (a)	$1.85 - 0.25 / 2 = 0.8 \text{ m}$	$1.6 - 0.25 / 2 = 0.675 \text{ m.}$
$M_u = q_{nu} \times a^2 / 2$	65.44 kN.m	62.31 kN-m
d required = SQRT($M_u / (0.138 \times f_{ck} \times b)$)	$\text{SQRT}(65.44 / (0.138 \times 20 \times 1000)) = 154 \text{ mm}$	$\text{SQRT}(62.31 / (0.138 \times 20 \times 1000)) = 150 \text{ mm}$
Overall depth D = d + cover 60 mm	214 mm	210 mm

01 M

01 M

01 M

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		Provide $A_{st} = 0.5 \times f_{ck} \times b \times d \{1 - \sqrt{1 - (4.6 \times \mu_u) / (f_{ck} \times b \times d^2)}}\} / f_y$	$D = 220 \text{ mm} \ \& \ d = 160 \text{ mm}$ $0.5 \times 20 \times 1000 \times 160 \{1 - \sqrt{1 - (4.6 \times 65.44 \times 10^6) / (20 \times 1000 \times 160^2)}}\} / 415 = 1380.5 \text{ mm}^2$	$D = 220 \text{ mm} \ \& \ d = 160 \text{ mm}$ $0.5 \times 20 \times 1000 \times 160 \{1 - \sqrt{1 - (4.6 \times 62.31 \times 10^6) / (20 \times 1000 \times 160^2)}}\} / 415 = 1297.5 \text{ mm}^2$	01 M
		Spacing for 16 mm dia. Bars = $1000 \times A_1 / A_{st}$	145.6 mm	155 mm	01 M
		Provided	16 mm dia. @ 140 mm c/c	16 mm dia. @ 150 mm c/c	01 M for fig.
Q.6	(a)	<p>Attempt any FOUR: An R.C. T-beam section reinforced for tension has the following dimension $b_f = 1250 \text{ mm}$, $b_w = 300 \text{ mm}$, $d = 550 \text{ mm}$, $D_f = 100 \text{ mm}$, $A_{st} = 1884 \text{ mm}^2$. Use of M20 & steel Fe415 is made. Calculate the limiting moment of resistance.</p> <p>Ans $D_f = 100 \text{ mm}$, $b_f = 1250 \text{ mm}$, $b_w = 300 \text{ mm}$, $d = 550 \text{ mm}$, $A_{st} = 1884 \text{ mm}^2$, M-250, Fe-415.</p> <p>Actual neutral axis $x_u = (0.87 \times f_y \times A_{st}) / (0.36 \times f_{ck} \times b_f)$ $= (0.87 \times 415 \times 1884) / (0.36 \times 20 \times 1250)$ $= 75.58 \text{ mm.}$ $x_{u\max} = 0.48 \times d$ $= 0.48 \times 550$ $= 264 \text{ mm.}$ $x_u < x_{u\max}$, hence beam is under reinforced.</p> <p>$\mu_u = 0.87 \times f_y \times A_{st} (d - 0.42x_u)$ $= 0.87 \times 415 \times 1884 (550 - 0.42 \times 75.58)$ $= 352.53 \times 10^6 \text{ N-mm.}$</p> <p style="text-align: center;">OR</p> <p>$\mu_u = 0.36 \times f_{ck} \times b_f \times x_u (d - 0.42x_u)$ $= 0.36 \times 20 \times 1250 \times 75.58 (550 - 0.42 \times 75.58)$ $= 352.53 \times 10^6 \text{ N-mm}$</p> <p>1)</p>			(16)
	Ans				01 M
					01 M
					02 M
Q.6	(b)	<p>State the I.S. specification for,</p> <p>i) Maximum reinforcement in beams & slabs. ii) Minimum reinforcement in slab. iii) Minimum shear reinforcement. iv) Cover to reinforcement in beam and slab.</p>			
	Ans	<p>i. Maximum reinforcement in slab and beam = 4% of gross area. $(0.04 \times b \times D)$</p> <p>ii. Minimum reinforcement in slab = 0.15 % for M.S. and 0.12% for deformed bars, of gross area.</p> <p>iii. Minimum shear reinforcement, $[A_{sv} / (b \times sv)] \geq [0.4 / (0.87 \times f_y)]$</p> <p>iv. Cover to reinforcement in beams & slab. For beams, 20 mm to 70 mm depending upon fire resistance required. For slabs, 20 mm to 55 mm depending upon fire resistance required.</p>			01 M
					01 M
					01 M
					01 M
Q.6	(c)	<p>Calculate effective flange width for T-beam for following details. Width of web = 230 mm.</p>			



	Ans	<p>Slab thickness = 100 mm. Size of hall = 12 m x 6 m. Width of support for beam = 230 mm. C/c spacing of beams = 3 m.</p> <p>bw = 230 mm, Df = 100 mm, Hall size = 12 m x 6 m., Support = 230 mm, C/c spacing of beam = 3 m.</p> <p>$l_e = 6 + 0.23 = 6.23 \text{ m.}$ Hence $l_0 = 6.23 \text{ m.}$ $bf = (l_0/6) + bw + 6Df$ $= (6230/6) + 230 + 6 \times 100$ $= 1868.3 \text{ mm.} < \text{C/c spacing (3000 mm)}$ Hence $bf = 1868.3 \text{ mm.}$</p>	01 M 02 M 01 M
Q.6	(d) Ans	<p>Write four I.S. specifications for the longitudinal reinforcement in columns.</p> <ol style="list-style-type: none">1. Minimum area of longitudinal reinforcement = 0.8% of gross area.2. Maximum area of longitudinal reinforcement = 6.0% of gross area.3. Minimum number of bars = 04 for square column, 06 for circular column and 06 for column with helical reinforcement.4. Minimum diameter of bar = 12 mm.5. Maximum spacing of bars measured along periphery of column = 300 mm.	Any four, 01 M for each
Q.6	(e) Ans	<p>Calculate the area of longitudinal steel for short circular column of diameter 400 mm with effective length 4.5 m to carry a factored load of 900 kN. Use M20 and Fe500.</p> <p>Column 400 mm diameter, $l_e = 4.5 \text{ m}$, $P_u = 900 \text{ kN}$, M-20, Fe-500.</p> <p>$A_g = \pi \times 400^2 / 4 = 125663.71 \text{ mm}^2$ $A_c = A_g - A_{sc} = 125663.71 - A_{sc}$ $P_u = (0.4 \times f_{ck} \times A_c) + (0.67 \times f_y \times A_{sc})$ $900 \times 10^3 = [0.4 \times 20 \times (125663.71 - A_{sc})] + (0.67 \times 500 \times A_{sc})$ $= 1005309.68 - 8A_{sc} + 335A_{sc}$ $A_{sc} = (900 \times 10^3 - 1005309.68) / 327$ $= (-) 322 \text{ mm}^2.$</p> <p>Required area of compression steel is negative; hence minimum area of steel is to be provided. Min. $A_{sc} = 0.8 \times 125663.71 / 100 = 1005.3 \text{ mm}^2.$ Provide $A_{sc} = 1005.3 \text{ mm}^2$</p>	01 M 02 M 01 M